CONTRIBUTION NO. **3731** FROM THE ARTHUR AMOS NOYES LABORATORY OF CHEMICAL PHYSICS, CALIFORNIA INSTITUTE OF TECHNOLOGY, PASADENA, CALIF. 91109

# The Crystal Structure of  $\mu$ -Amido- $\mu$ -superoxo-bis [tetraamminecobalt(III)]  $\text{Tetrantrate}, \; [(\text{NH}_3)_4\text{Co}(\text{NH}_2)(\text{O}_2)\text{Co}(\text{NH}_3)_4\,](\text{NO}_3)_4$

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The crystal and molecular structure of  $\mu$ -amido- $\mu$ -superoxo-bis[tetraamminecobalt(III)] tetranitrate,  $(NH_3)_4Co(NH_2)$ - $(O_2)Co(NH_3)_4$ <sup>4+</sup> $(O_3^-$ , has been determined by X-ray crystallographic analysis. The green-black salt crystallizes in the monoclinic space group **P2<sub>1</sub>/c** with unit cell dimensions  $a = 8.451 \pm 0.003 \text{ Å}$ ,  $b = 13.196 \pm 0.006 \text{ Å}$ ,  $c = 17.304 \pm 0.003 \text{ Å}$ ,  $\beta = 103.90 \pm 0.03^{\circ}$ , and  $Z = 4$ . The measured density is  $1.95 \pm 0.01$  g/cm<sup>3</sup>; the calculated density is  $1.947 \pm 0.001$  g/ cm<sup>3</sup>. Intensity data were collected with a Datex-automated General Electric diffractometer using Fe K $\alpha$  radiation. The structure was determined by Patterson methods and refined by three-dimensional Fourier and least-squares techniques. Refinement of all positional and thermal parameters (hydrogen atoms isotropic) yielded a final *R* index of 0.051 for 1888 reflections. The coordinating ligands form nearly regular octahedra about the cobalt atoms, with Co-N and Co-O distances of about **1.96** and **1.87 A.** The five-membered ring co-N-co-0-0- is very nearly planar; the *0-0* distance is **1.32 A,** and the Co-N-Co and Co-0-0 angles are 115 and **120°,** respectively. This geometry indicates that the *02* bridge is a superoxo rather than a peroxo group.

#### **Introduction**

Dinuclear cobalt complexes have been known for some time; the major analytical, preparative, and constitutional work was carried out by Alfred Werner and his coworkers at about the turn of the century. These compounds may be prepared with from one to three bridging groups which can be one or more of the following: OH<sup>-</sup>, NH<sub>2</sub><sup>-</sup>, CH<sub>3</sub>COO<sup>-</sup>, NO<sub>2</sub><sup>-</sup>, SO<sub>4</sub><sup>2</sup><sup>-</sup>,  $C_2O_4^{2-}$ ,  $O_2^{2-}$ ,  $O_2^-$ , and  $O_2H^-$ .

The compounds containing  $O<sub>2</sub>$  bridges are of particular interest as they exhibit involved oxidation-reduction behavior and complicated interconversion reactions which may have relevance to the understanding of the behavior of biologically important molecular oxygen carriers. Our particular interest in these compounds stemmed from the unresolved nature of the bonding in and the configuration of the *02* bridge and from the several different structures for these bridged cations that had been proposed in the literature.

The following monobridged and analogous dibridged dicobalt complexes were investigated by Werner<sup>1,2</sup>



The salts of I and I11 are generally red or brown and those of I1 and IV are dark green. In Werner's formulation the  $O<sub>2</sub>$  groups in all of these complexes were assumed to be peroxo groups. This formulation quite satisfactorily resulted in the cobalt atoms in I and I11 all being tervalent, but it required that I1 and IV each contain one tervalent and one tetravalent cobalt atom.

Werner was unable to give any further proof of the existence of tetravalent cobalt.

The cations II and IV were shown by Gleu<sup>3</sup> and Malatesta4 to be paramagnetic with a magnetic moment consistent with the presence of one unpaired electron. Esr studies of I1 and IV in solution have demonstrated that the unpaired electron spends an equal fraction of its time on each cobalt atom. $5,6$  This suggests that IV, for example, may be a resonance hybrid of V and VI, with each cobalt atom having a valency inter-



mediate between three and four, $4$  or, alternatively, that the unpaired electron may occupy a molecular orbital which, although centered on the  $O<sub>2</sub>$  bridge, extends well onto the cobalt atoms. In the first formulation the  $O<sub>2</sub>$  bridge is still a peroxide group, as was originally assumed, but in the second case the bridge possesses more the character of an  $O_2$ , or superoxide, group.

On the basis of single-crystal esr measurements, Goodman, Hecht, and Weil<sup>7</sup> tentatively predicted that the  $O_2$  bridge in IV would be  $\sigma$  bonded to each of the cobalt atoms and oriented skew to the Co-Co axis, as indicated in Figure la. This configuration is quite

**<sup>(1)</sup> A. Werner and** A. **Mylius,** *2. Anorg. Allgem. Chem.,* **16, 245 (1898).** 

**<sup>(2)</sup> A. Werner, Ann.** *Chem.,* **376,** 1 **(1910).** 

**<sup>(3)</sup> K. Gleu,** *Angem. Chem.,* **48, 470 (1935).** 

**<sup>(4)</sup> L. Malatesta,** *Gazz. Chim. Ital.,* **79, 287 (1942).** 

*<sup>(5)</sup>* **I. Bernal, E. A. B. Ebsworth, and** J. **A. Weil,** *PYOC. Chem.* Soc., **57**   $(1959).$ 

**<sup>(6)</sup> E. A.** V. **Ebsworth and** J. A. **Weil,** *J. Phys. Chem.,* **63, 1890 (1955).** 

**<sup>(7)</sup> G. Goodman, H. Hecht, and** J. **A. Weil, "Free Radicals in Inorganic Chemistry," Advances in Chemistry Series, No. 36, American Chemical Society, Washington, D.** *C.,* **1962, p 90.** 





Figure 1.-The proposed configurations of the ring formed by the two cobalt atoms and the two bridges. The ammine groups coordinated to the cobalt atoms have been omitted for clarity: (a) the configuration expected when the  $O_2$  bridge is a  $\sigma$ -bonded peroxide group; (b) the configuration expected if the *02* bridge is considered to be perpendicular to the  $Co-N-Co$  plane and  $\pi$  bonded to the cobalt atoms; (c) the planar configuration predicted assuming the  $O_2$  bridge to be a superoxide group, which was confirmed by this study.

close to what would be expected if the *02* bridge were a peroxide group; the five-membered ring formed by the two cobalt atoms and the atoms of the bridges would have to be decidedly nonplanar in order to accommodate the relatively large dihedral angle expected for a peroxide group.

From steric considerations and electrochemical data Vlček proposed that the most probable configuration for IV would be one in which the *02* bridge is oriented perpendicular to the Co-Co axis and bonded to the cobalt atoms by the overlap of its  $\pi$  orbitals with the cobalt d orbitals<sup>8</sup> (Figure 1b). Such  $\pi$  bonding would presumably be similar to that found in metal-olefin complexes, in the iridium-oxygen complexes studied by Ibers,<sup>9</sup> or in the anion of  $K_3CrO_8$ ; this last was interpreted by Pauling as containing four *02* groups having mostly superoxide character. **lo** 

**A** third configuration, with the *02* bridge coplanar with the Co-N-Co grouping (Figure IC), would result if the  $O_2$  bridge were assumed to be a  $\sigma$ -bonded superoxide group. Such a configuration would further be in agreement with the planar bridge structure recently re-

ported for the cation of the analogous monobridged compound, II.<sup>11,12</sup>

This structural study was undertaken in order to determine the exact configuration of cation IV and in particular to determine the geometry of the  $O<sub>2</sub>$  bridge.

# Experimental Section

Vortmann's sulfate, a mixture containing the cations



was prepared by the method given by Werner,<sup>13</sup> and from it samples of  $\mu$ -amido- $\mu$ -superoxo-bis[tetraamminecobalt(III)]tetranitrate were extracted with concentrated nitric acid. The samples obtained were washed with a little dilute nitric acid, then with alcohol, and then dried. Crystals of the compound were prepared by allowing a test tube of hot, saturated nitrate solution about  $2$   $F$  in nitric acid to cool slowly overnight in a thermos of hot water. The dark green-black crystals grown in this fashion were generally extremely thin blades which appeared to be hollow. A number of smaller, slightly stockier blades were also formed from which the crystals used in this structure analysis were chosen.

The compound was also found to crystallize in a second modification from more acidic nitric acid solutions *(ca.* 8-10 *F).* These crystals were obtained in the form of small "stars" consisting of about 12 needlelike crystals radiating from a central point. Weissenberg photographs of single needles of these crystals indicated that they were all twinned. They were monoclinic with approximate unit cell dimensions:  $a = 8.0$ ,  $b = 18.6$ ,  $c = 12.4$ A. The monoclinic angle was not determined, but it is quite close to 90".

The space group  $P2_1/c$  was indicated by the systematic absences on Weissenberg photographs of reflections *h01* with *<sup>I</sup>* odd and *OkO* with *k* odd. The cell constants were determined by a least-squares fit to measurements of  $2\theta$  for 67 reflections on photographs prepared with a special camera which holds the film in the asymmetric position. The resulting values, their standard deviations, and related data are:  $a = 8.451 \pm 0.003$  $\AA$ ,  $b = 13.196 \pm 0.006$   $\AA$ ,  $c = 17.304 \pm 0.003$   $\AA$ ,  $\beta = 103.90 \pm 0.003$  $0.03^\circ$ ,  $\lambda$ (Cu *Ka*<sub>1</sub>)  $1.54051 \text{ Å}$ ,  $\lambda$ (Cu *Ka*<sub>2</sub>)  $1.54433 \text{ Å}$ ),  $V = 1873 \text{ Å}^3$ , and  $T = 26^\circ$ . The density calculated for four formula units of  $Co_2(NH_2,O_2)(NH_3)_{8}(NO_3)_{4}$  per unit cell is 1.947  $\pm$  0.001 g cm<sup>-1</sup>; the density determined by flotation in a carbon tetrachloride-1,2-dibromoethane solution is  $1.95 \pm 0.01$  g cm<sup>-1</sup>.

A nearly rectangular prism about 0.05  $\times$  0.07  $\times$  0.04 mm in size was used for the collection of three-dimensional intensity data. The intensities were measured using a  $\theta$ -2 $\theta$  scan at a scanning speed of  $1^{\circ}/$ min. Background was counted for 100 sec at each end of the scan. The scan range of about  $2^\circ$  was adjusted to account for  $\alpha_1-\alpha_2$  splitting. The takeoff angle used was 3°; a check of several high-angle reflections showed that our settings included the entire peak in the scan.

Iron radiation  $(\lambda(K\alpha)$  1.9373 Å) filtered with a single thickness of Du Pont manganese dioxide (General Electric Part Xo. 257) was used to reduce absorption and fluorescence effects. The temperature in the laboratory containing the diffractometer was fairly constant at 27° throughout the collection of the data.

**A** moderately strong reflection, 225, was chosen as a "check" reflection and was remeasured after every **15** reflections. There were no significant deviations in the intensity of this reflection during the collection of the data, which required approximately 12 days of 24-hr operation. Of the 1993 measured reflections, 1888 were calculated as greater than zero and were used in the refinement of the structure.

<sup>(8)</sup> **A. A.** Week, *Tvans. Favaday Soc.,* **56,** 11'37 (1960).

<sup>(9)</sup> J. **A.** McGinnety, R. J. Doedens, and J. **A.** Ibers, *Inovg. Chem.,* **6,** 2243 (1967).

<sup>(10)</sup> L. Pauling, "The Nature of the Chemical Bond," 34th ed, Cornel1 University Press, Ithaca, N. *Y.,* 1960, **pp** 351, 352.

<sup>(11)</sup> W. P. Schaefer and R. E. Marsh, *Acta Cvyst.,* **21,** 735 (1966).

<sup>(12)</sup> R. E. Marsh and **W.** P. Schaefer, *ibid.,* **B24,** 246 (1968).

<sup>(13)</sup> **A.** Werner, *Bev.,* **40,** 4609 (1907).

# Treatment of the Data

The values for the observed intensities,  $I_{\text{obsd}}$ , were derived from the scaler counts using the formula

$$
I_{\text{obsd}} = S - \frac{B_1 + B_2}{2} \left( \frac{t}{100} \right)
$$

where *S* is the scan count,  $B_1$  and  $B_2$  are the two background counts, and *t* is the scan time in seconds. Negative values of  $I_{\text{obsd}}$  calculated from this formula were set equal to zero.

The standard deviation for each reflection was calculated using

$$
\sigma^2(I_{\text{obsd}}) = S + \frac{B_1 + B_2}{2} \left(\frac{t}{100}\right)^2 + (0.03S)^2
$$

The last term in this equation is an empirical term (Busing and Levy14) which presumably allows for errors not due to counting statistics. The intensities and their standard deviations were corrected for Lorentz and polarization factors but not for absorption. The value of  $\mu$  for this compound is 59 cm<sup>-1</sup>, and neglect of this correction could have led to errors of  $4\%$  in the structure factors in the extreme case. The standard deviations calculated in this way were the basis for the weights used in the least-squares refinement.

## Determination and Refinement of the Structure

A three-dimensional Patterson synthesis was calculated and from it the approximate coordinates of the cobalt atoms were found. Structure factors calculated on the basis of these coordinates led to an *R* index  $(R =$  $\Sigma||F_{o}$  –  $|F_{e}||/[\Sigma]F_{o}]$  of 0.44. A three-dimensional electron density synthesis was then computed; all of the nonhydrogen atoms were apparent in this synthesis, and two cycles of full-matrix, least-squares refinement of the coordinates and isotropic temperature factors of all of these atoms reduced the *R* index to 0.11, Introducing anisotropic temperature factors for the cobalt atoms further reduced the *R* index to 0.10. At this point difference maps were calculated in the planes where the hydrogen atoms of the  $NH<sub>3</sub>$  groups were expected; nearly all of the hydrogen atoms were apparent, and they were included in subsequent calculations.

In subsequent least-squares cycles, 367 parametersa scale factor, a secondary extinction factor,  $15$  positional parameters of all of the atoms, anisotropic temperature factors for the nonhydrogen atoms, and isotropic temperature factors for the hydrogen atoms-were adjusted. Because of the storage limitations of the computer, these 367 parameters were apportioned among four complete matrices.

All calculations were carried out on an IBM 7094 computer using subprograms operating under the CRYM crystallographic computing system. The quantity minimized in the least-squares calculations was



Figure 2.-Bond distances for the cation.

 $\sum w (F_0^2 - F_0^{*2})^2$ , where  $w = 1/\sigma^2 (F_0^2)$ , and  $F_0^*$  is as defined by Larson's eq **3.15b** Atomic form factors for cobalt, nitrogen, and oxygen were taken from ref 16, the values for Co being reduced by 1.74 electrons to take account of anomalous dispersion," and the form factor for hydrogen was that calculated by Stewart, Davidson, and Simpson.<sup>18</sup>

In the final cycle, no heavy-atom parameter shifted by as much as 0.5 esd. The final *R* index for 1888 "observed" reflections was 0.051, and the goodness of fit,  $[\Sigma w (F_0^2 - F_0^2)^2/(m - s)]^{1/2}$ , was 1.32. The final value of the secondary extinction parameter g, as defined by Larson's eq 3,<sup>15b</sup> was  $(1.25 \pm 0.19) \times 10^{-6}$ .

Table I contains the observed and calculated structure factors. The final parameters and their standard deviations for the heavy atoms are given in Table 11, and the parameters of the hydrogen atoms are given in Table 111.

The estimated standard deviations in the positions of the cobalt atoms are approximately 0.001 A, while the esd's for the ammine nitrogen atoms and the bridge oxygen atoms are about  $0.004$  Å. The estimated standard deviations in the positions of the nitrate group atoms are roughly 0.008 Å, but these are not especially meaningful because the vibrational amplitudes for some of the nitrate oxygen atoms exceed 0.4 A.

#### Description and Discussion of the Structure

Contrary to the predictions of Goodman, Hecht, and Weil<sup>7</sup> and of Vlček,<sup>8</sup> the  $O_2$  bridge is very nearly coplanar with the cobalt atoms; the sum of the angles in the ring formed by the cobalt atoms and the bridges is 539.6', only 0.4" from the total expected for a planar, five-membered ring. The two oxygen atoms each lie 0.045 A from, and on opposite sides of, the Co-N-Co plane. Since these distances are roughly 10 times the estimated standard deviations in the oxygen positions, the distortion is real; it is probably due mainly to bondangle strain in the five-membered ring.

The bond distances for the  $\mu$ -amido- $\mu$ -superoxo-bis-[tetraamminecobalt $(III)$ ] cation are shown in Figure 2;

<sup>(14)</sup> W. R. Busing and H. **A.** Levy, *J.* **Chem.** *Phys.,* **26,** 563 (1957).

**<sup>(15)</sup>** (a) **W. H.** Zachariasen, *Acta Cvyst.,* **16,** 1139 (1963); (b) **A.** Larson, *ibid.,* **23,** 664 (1967).

<sup>(16)</sup> "International Tables for X-Ray Crystallography," Vol. 3, The (17) D. Cromer, *Acta* **Crysl., 18,** 17 (1965). *Af'* = -1.74 electrons; Kynoch Press, Birmingham, England, 1962, pp **202-204.** 

 $\Delta f'' = 0.8$  electron was ignored in this centric structure.

<sup>(18)</sup> R. F. Stewart, E. R. Davidson, and W. T. Simpson, *J. Chem. Phys.,*  **42,** 3175 (1965).



TABLE I<sup>a</sup>

<sup>*a*</sup> The four parts in each column are *h*,  $10F_0$ ,  $10\sigma(F_0)$ , and  $10F_0$ . The symbol --- in the  $F_0$  column indicates that  $F_0$  was assigned the value 0; asterisks in the column of standard deviations indicate the reflections were not used in the refinement.

the angles are listed in Table IV. The *0-0* distance of 1.320 *8* is not significantly different from the values 1.317 and 1.312 A found for the *0-0* distance in two salts of the analogous singly bridged superoxo cation<sup>11,12</sup> and is very close to the 1.2s-8 *0-0* distance found for the superoxide ion.<sup>10</sup> Pauling considers the superoxide oxygen-oxygen bond as a combination of a single  $(\sigma)$ bond and a three-electron  $(\pi)$  bond.<sup>10</sup> Since two orbitals are utilized in the oxygen-oxygen bond, it is impossible for this anion to form any type of bridged compound other than a planar one.

Interpreting the *02* bridge in this compound as a superoxo bridge satisfactorily accounts for the observed esr spectra since the unpaired electron can be expected to be delocalized over the bridge so that it can interact equally with the nuclear spins of both cobalt atoms. Recent esr measurements by Weil and Kinnaird on samples of this compound, in which <sup>17</sup>O was incorpo-



<sup>a</sup> The temperature factors are of the form  $\exp[-(b_{11}h^2 + b_{22}k^2 +$  $b_{33}l^2 + b_{12}hk + b_{13}hl + b_{23}kl$ ). All values have been multiplied by 10<sup>4</sup>.

# TABLE **I11**  POSITIONAL AND THERMAL PARAMETERS OF THE HYDROGEN ATOMS<sup>a</sup>



TABLE IV

DISTANCES AND ANGLES IN THE CATION<sup>a</sup>



**<sup>a</sup>**Values in parentheses are estimated standard deviations in the last digits.



rated into the bridge, indicate that this is indeed the case; $19$  the unpaired electron appears to reside in what amounts to a molecular orbital over the Co-0-0-Co atoms with the nodal plane coincident with the plane of the ring.

Thewalt and Marsh, in their study of the ethylenediamine form of this compound, have found the *Co-0-*  0-Co-N- ring to be similarly planar although slightly more puckered than in the ammine-complexed form we have studied, with an O-O bond distance of 1.36 Å.<sup>20</sup> This slightly longer *0-0* distance is consistent with the larger deviation from planarity of the ring and the consequent weakening of the half-order bond.

There are four nitrate groups per asymmetric unit. The bond distances and angles within these groups are given in Table V. The average N-0 distance for all of

(19) *J.* A. Weil and J. K. Kinnaird, *J. Phys. Chem.,* **71,** 3341 (1967).

**a** Values of *x*, *y*, and *z* have been multiplied by 10<sup>8</sup>. (20) U. Thewalt and R. E. Marsh, *J. Am. Chem. Soc.*, **89**, 6364 (1967).



### TABLE VI1

BOND ANGLES (AND STANDARD DEVIATIONS) INVOLVING THE HYDROGEN ATOMS

Atoms	Angle, deg	Atoms	Angle, deg	
$Co(1)-N(1)-H(1)$	108(3)	$H(12) - N(5) - H(13)$		102(5)
$Co(1)-N(1)-H(2)$	112(3)	$H(12) - N(5) - H(14)$		113(5)
$Co(2)-N(1)-H(1)$	115(3)	$H(13)-N(5)-H(14)$		101(5)
$Co(2)-N(1)-H(2)$	109(3)	$Co(2)-N(6)-H(15)$		109(5)
$H(1)-N(1)-H(2)$	96(4)	$Co(2)-N(6)-H(16)$		122(5)
$Co(1)-N(2)-H(3)$	110(5)	$Co(2)-N(6)-H(17)$		116(4)
$Co(1)-N(2)-H(4)$	119(4)	$H(15) - N(6) - H(16)$		113(7)
$Co(1)-N(2)-H(5)$	112(4)	$H(15)-N(6)-H(17)$		96(6)
$H(3)-N(2)-H(4)$	109(7)	$H(16)-N(6)-H(17)$		98(6)
$H(3)-N(2)-H(5)$	104(6)	$Co(2)-N(7)-H(18)$		124(11)
$H(4)-N(2)-H(5)$	104(6)	$Co(2)-N(7)-H(19)$		110(6)
$Co(1)-N(3)-H(6)$	103(5)	$Co(2)-N(7)-H(20)$		120(5)
$Co(1)-N(3)-H(7)$	117(5)	$H(18)-N(7)-H(19)$		119 (12)
$C_0(1) - N(3) - H(8)$	117(6)	$H(18) - N(7) - H(20)$		96(12)
$H(6)-N(3)-H(7)$	87(7)	$H(19)-N(7)-H(20)$		78 (9)
$H(6)-N(3)-H(8)$	107(8)	$Co(2)-N(8)-H(21)$		114 (5)
$H(7)-N(3)-H(8)$	119(8)	$Co(2)-N(8)-H(22)$		110(7)
$Co(1)-N(4)-H(9)$	121(5)	$Co(2)-N(8)-H(23)$		110(11)
$Co(1)-N(4)-H(10)$	110(4)	$H(21) - N(8) - H(22)$		117(9)
$Co(1)-N(4)-H(11)$	111(6)	$H(21) - N(8) - H(23)$		102(12)
$H(9)-N(4)-H(10)$	121(6)	$H(22) - N(8) - H(23)$		103(13)
$H(9)-N(4)-H(11)$	94(7)	$Co(2)-N(9)-H(24)$		122(5)
$H(10) - N(4) - H(11)$	94(7)	$Co(2)-N(9)-H(25)$		110(4)
$Co(1)-N(5)-H(12)$	112(3)	$Co(2)-N(9)-H(26)$		114 (7)
$Co(1)-N(5)-H(13)$	112(4)	$H(24)-N(9)-H(25)$		91(6)
$Co(1)-N(5)-H(14)$	115(3)	$H(24)-N(9)-H(26)$		111(9)
		$H(25)-N(9)-H(26)$		104(8)

the nitrate groups is 1.24 *8,* a value slightly higher than expected but not significantly so in view of the relatively higher standard deviations of the atomic positions compared with those of the cation atoms.

Three of the nitrate groups are planar well within experimental error. The nitrate group containing  $N(13)$ , however, appears to be significantly nonplanar, the nitrogen atom being located about  $0.1 \text{ Å}$  above the plane of the oxygen atoms. The large thermal vibration amplitudes for the atoms of this group, all nearly 0.4 A and perpendicular to the plane of the oxygen atoms, and the possibilities for the formation of alternative hydrogen bonds suggest that this nitrate group is either partially disordered or that it is confined in a very wide and shallow potential well which permits it to vibrate freely with such large amplitudes.

TABLE VIII HYDROGEN-BONDING SCHEME Bonded atoms N-O distance,  $\AA$  Bonded atoms N-O distance,  $\AA$  $N(1)-H(1)-O(8)$  3.111  $N(5)-H(14)-O(8)$  2.920  $N(1)-H(2)-O(12)$ f 3.284  $N(6)-H(15)-O(5)$ <sup>e</sup> 3.158  $N(2)-H(3)-O(13)$ <sup>c</sup> 3.003  $N(6)-H(16)-O(7)$  2.991  $N(2)-H(4)-O(4)h$  2.929  $N(6)-H(17)-O(9)$  3.030<br> $N(2)-H(5)-O(9)g$  3.003  $N(7)-H(18)-O(14)g$  3.256  $N(7)-H(18)-O(14)'$  3.256  $N(3)-H(6)-O(6)$ <sup>o</sup> 3.283  $N(7)-H(19)-O(9)$  3.368  $N(3)-H(7)-O(7)^{c}$  3.222  $N(7)-H(20)-O(6)^{b}$  3.200<br> $N(3)-H(8)-O(11)^{d}$  2.966  $N(8)-H(21)-O(11)$  3.035  $2.966 \qquad N(8)-H(21)-O(11) \quad 3.035$  $N(4) - H(9) - O(12)$ <sup>c</sup> 3.052  $N(8) - H(22) - O(5)$ <sup>e</sup> 3.137  $N(4)-H(10)-O(12)'$  3.027  $N(8)-H(23)-O(14)^{b}$  3.195<br> $N(4)-H(11)-O(3)^{a}$  3.089  $N(9)-H(24)-O(8)^{b}$  3.106 3.089  $N(9) - H(24) - O(8)^{b}$  3.106  $N(5)-H(12)-O(6)$ <sup>2</sup> 2.989  $N(9)-H(25)-O(10)$ <sup>2</sup> 3.289  $N(5)-H(13)-O(10)^d$  3,097  $N(9)-H(26)-O(5)^h$  2,921

 $a-h$  Oxygen positions other than the *x*, *y*, *z* in Table II: (a)  $x - 1$ ,  $y, z$ ; (b)  $x + 1$ ,  $y, z$ ; (c)  $x, \frac{1}{2} - y, z - \frac{1}{2}$ ; (d)  $x - 1$ ,  $\frac{1}{2} - y, z - \frac{1}{2}$ ; (e)  $x, \frac{1}{2} - y, z + \frac{1}{2}$ ; (f)  $1 - x, y - \frac{1}{2}, \frac{1}{2} - z$  $x - 1$ , y, z; (b)  $x + 1$ , y, z; (c)  $x$ ,  $\frac{1}{2} - y$ ,  $z - \frac{1}{2}$ ; (d)  $x - 1$ ,  $\binom{1}{2} - y, \, \bar{z} - \binom{1}{2}; \, \text{(e)} \, x, \, \frac{1}{2} - y, \, \bar{z} + \frac{1}{2}; \, \text{(f)} \, 1 - z; \, \text{(g)} \, 1 - x, \, \bar{y} + \frac{1}{2}, \, \frac{1}{2} - z; \, \text{(h)} \, 2 - x, \, -y, \, -z.$ 





*<sup>a</sup>*Values in parentheses are estimated standard deviations.

The hydrogen positions as obtained from the leastsquares refinement are, in general, chemically reasonable. The bond distances and angles involving the hydrogen atoms are given in Tables VI and VII. Although the calculated N-H distances range down to  $0.52$  Å, the shorter values pertain to those hydrogen atoms having large temperature motions and, concomitantly, large standard deviations in their positions.

The ions appear to be held together in the crystal by a network of hydrogen bonds. The lengths of most of



Figure 3.—The thermal motion of the cation. Thermal ellipsoids are drawn at the 0.74 probability level.

the interactions we have characterized as hydrogen bonds are somewhat longer than the average value of  $2.88 \pm 0.13$  Å tabulated by Pimentel and McClellan<sup>21</sup> for bonds of the type  $N^+$ -H $\cdots$ O. The crowding between the many acceptor atoms surrounding each cation is perhaps responsible for the hydrogen bonds being longer than normal. Table VI11 lists what we consider to be **a** probable hydrogen-bonding scheme. The oxygen-atoms in the superoxo bridge appear to be the only oxygen atoms in the crystal that are not involved in hydrogen bonding. Space-filling atomic models show that these bridge atoms are thoroughly shielded by ammonia groups.

# Thermal Vibrations

The thermal vibrations of the atoms in the cation are in general what would be expected from a consideration of its geometry. The vibrations of the cobalt atoms and of the ring nitrogen atom are essentially isotropic with rms amplitudes of roughly  $0.15$  Å. The superoxo

(21) G. C. Pimentel and **A.** L. McClellan, **"The** Hydrogen Bond," W. H. Freeman and Co., San Francisco, Calif., 1960, **p** 289.

oxygen atoms have somewhat larger excursions perpendicular to the ring plane with rms amplitudes of about 0.20 *b.* The rms amplitudes of vibration of the ammine nitrogen atoms are between 0.15 and 0.23 Å with the maximum amplitudes in directions very nearly perpendicular to the Co-N bonds. These thermal motions can best be understood by looking at Figure 3.

The vibrations of the nitrate group atoms are significantly larger than those of the cation atoms, their rms amplitudes ranging from  $0.14$  to  $0.43$  Å and averaging about 0.21 **8.** The largest vibrations are generally perpendicular to the planes of the ions, particularly in the nitrate group containing  $N(13)$ . As was discussed previously, it appears as if this whole group is vibrating in a wide, shallow potential well.

No attempt was made to correct the bond lengths for thermal vibration. The rms displacements of the atoms along the principal axes of their thermal ellipsoids are given in Table IX.

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